

# Small area estimation of district-level fertility in sub-Saharan Africa

---

Oli Stevens  
Imperial College London  
6th April 2020

- District level estimates of fertility desired for:
  - Improved population projections at subnational levels
  - Estimation of children living with HIV
    - Key epidemic indicator
    - Resource allocation for prevention of mother-to-child transmission
  - Evaluation of family planning programmatic scaleup

**Objective** Estimate annual age-specific fertility rates at district level for SSA countries from household survey data

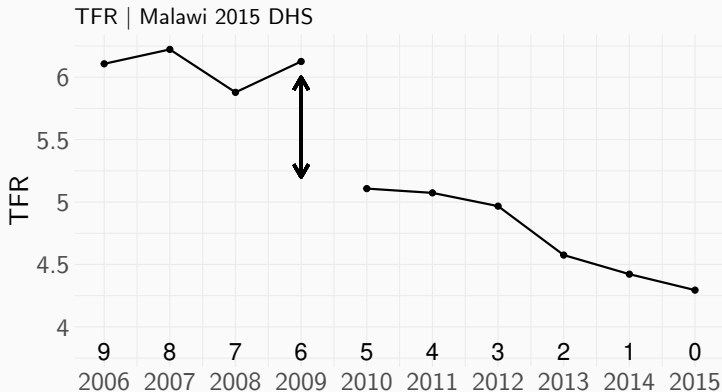
- Household surveys with full birth histories
  - Demographic Health Surveys (2000, 2004, 2010, 2015)
  - Malaria Indicator Survey (2012, 2014, 2017)
  - Multiple Indicator Cluster Survey (2006, 2013)
- Full birth history data:
  - DHS, MICS: 15 years
  - MIS: 5 years
- Summary birth histories from censuses - to be included

# Challenges

- Non sampling biases
  - Displacing
  - Omitting
- Data available at different spatial resolutions
  - DHS: geomasked coordinates → district
  - MICS: coordinates unavailable → province

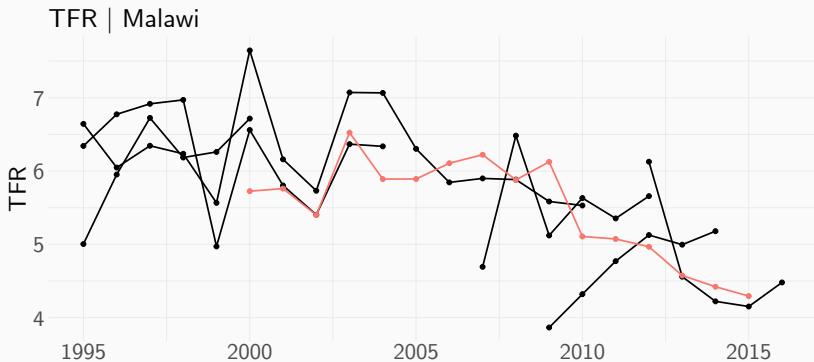
- DHS collects full birth histories for children in the 5 years preceding the survey, and an abbreviated question set thereafter
- Births are asked about “in the order in which they occurred”

# Data and workflow | Non-sampling bias in household surveys



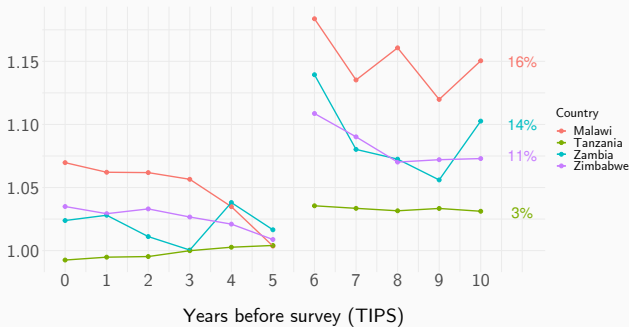
# Data and workflow | Non-sampling bias in household surveys

- Intersurvey analysis can estimate magnitude of bias due to overlap in recall periods (Masquelier, 2013; Schoumaker, 2014)



# Data and workflow | Non-sampling bias in household surveys

- Intersurvey analysis can estimate magnitude of bias due to overlap in recall periods (Masquelier, 2013; Schoumaker, 2014)
- $$Y_{a,t,tips} = \mu + \alpha_a + \gamma_t + \beta_1(TIPS > 5) + \omega_{tips}$$





## Model specification

$$b_{ait} \sim Po(\lambda_{ait} \cdot E_{ait})$$

$$\log(\lambda_{ait}) = \mu + \alpha_a + \gamma_t + \delta_i + \eta_{a,t} + \eta_{a,i} + \eta_{i,t}$$

Average log fertility rate:  $\mu \sim N(0, 5)$

Age pattern:  $\alpha_a \sim RW1(\sigma_\alpha^2)$        $a \in \{15 - 19, 20 - 24 \dots 45 - 49\}$

Time trend:  $\gamma_t \sim RW2(\sigma_\gamma^2)$        $t \in \{1995 : 2020\}$

Spatial correlation:  $\delta_i \sim BYM2(\sigma_\delta^2)$        $i \in \{1 \dots n_i\}$

$$b_{ait} \sim Po(\lambda_{ait} \cdot E_{ait})$$

$$\log(\lambda_{ait}) = \mu + \alpha_a + \gamma_t + \delta_i + \eta_{a,t} + \eta_{a,i} + \eta_{i,t}$$

$$\eta_{a,t} : AR1 \otimes AR1$$

$$\eta_{a,i} : AR1 \otimes ICAR$$

$$\eta_{i,t} : ICAR \otimes AR1$$

## Model specification

$$b_{ait} \sim Po(\lambda_{ait} \cdot E_{ait})$$

$$\log(\lambda_{ait}) = \mu + \alpha_a + \gamma_t + \delta_i + \eta_{a,t} + \eta_{a,i} + \eta_{i,t}$$

Observation model

$$\log(\tilde{b}_{ait}) = \log(\lambda_{ait} \times E_{ait}) + \beta_1 TIPS_d + \omega_{TIPS}$$

$$TIPS_d = \begin{cases} 0, & \text{if } TIPS < 5 \\ 1, & \text{otherwise} \end{cases}$$

$$\omega_{tips} \sim RW1(\sigma_\omega^2)$$

$$tips \in \{0 : 14\}$$

$$b_{ait} \sim Po(\lambda_{ait} \cdot E_{ait})$$

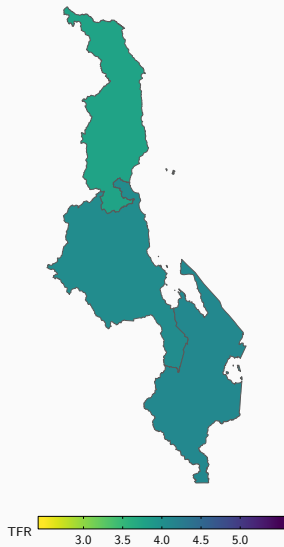
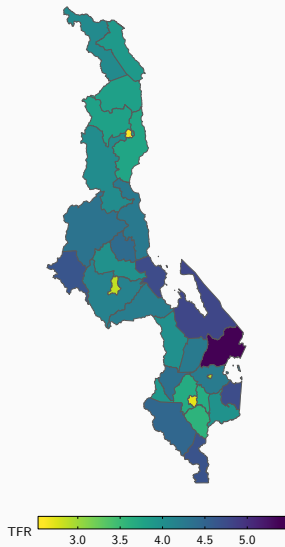
$$\log(\lambda_{ait}) = \mu + \alpha_a + \gamma_t + \delta_i + \eta_{a,t} + \eta_{a,i} + \eta_{i,t}$$

Aggregation model

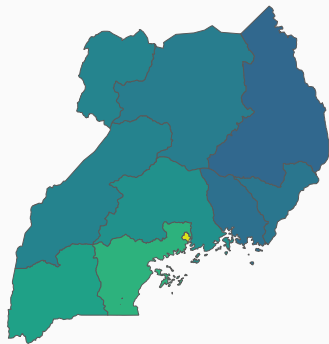
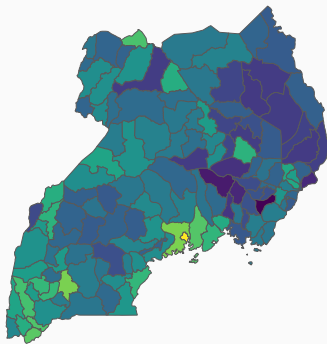
$$\log(\tilde{b}_{at}) = \frac{\sum_i \log(\lambda_{ait} \times E_{ait})}{E_{at}} + \beta_1 TIPS_d + \omega_{TIPS}$$

- Model fit in Template Model Builder (TMB)
- Countries take  $< 2$  minutes to fit and sample

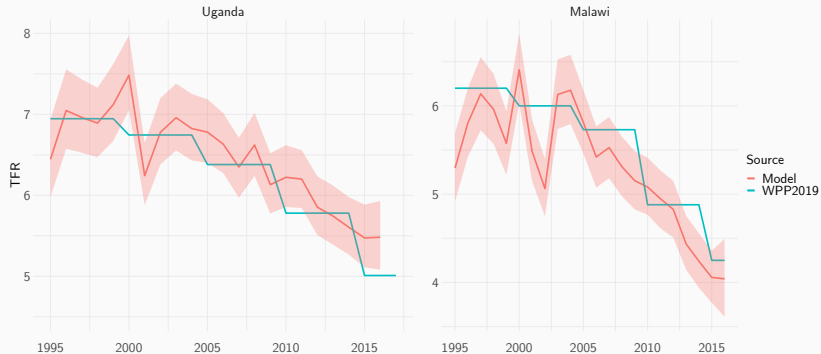
# Results



# Results



# Results





- There exists district-level heterogeneity that is not captured by admin-1 estimates
- Non-sampling bias can lead to substantial distortion of fertility estimates in surveys
  - Role of bias adjustment depends on measure of fertility
- Can be adjusted for within automated analysis
- Consideration of further non-sampling bias
  - Displacement of first birth(s) at older ages

- Structured model for fertility transition and projection (Alkema, 2011; Sevkicova, 2012)
- Survey random effects & multi-country fitting
- Census data, additional country-specific surveys, summary birth histories

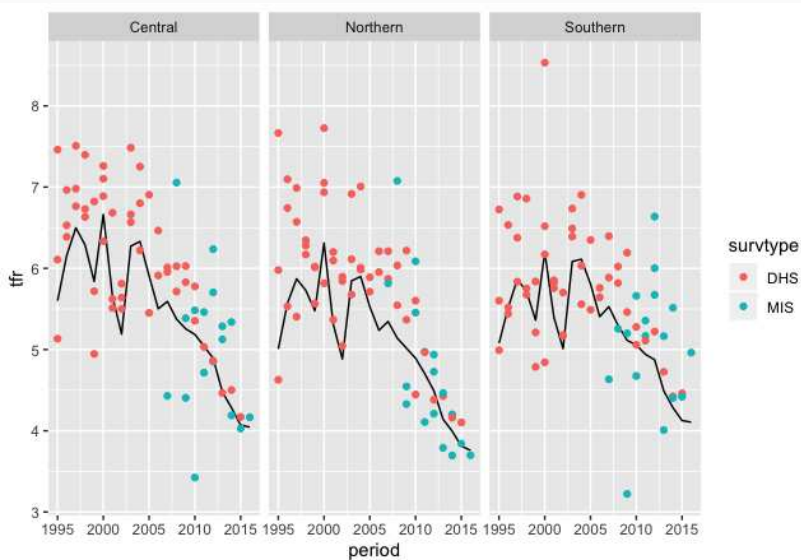
## **Small area estimation of district-level fertility in sub-Saharan Africa**

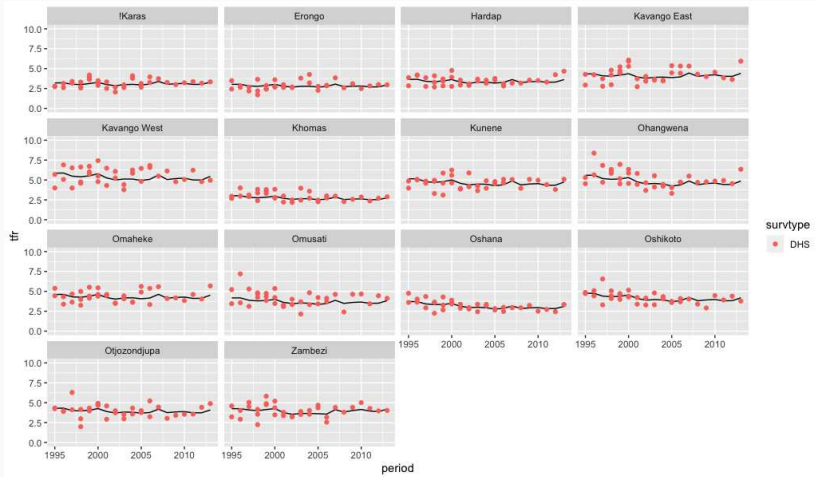
Oli Stevens

Imperial College London

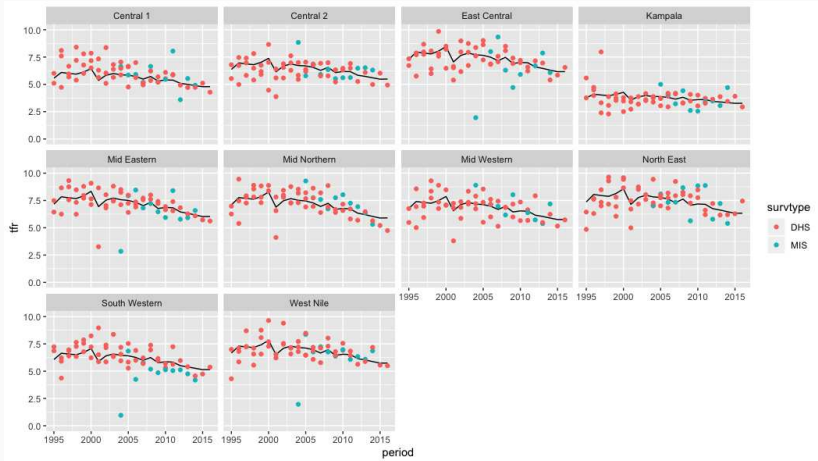
6th April 2020

# Extras





**Figure 2: NAM admin-1**



**Figure 3: UGA admin-1**

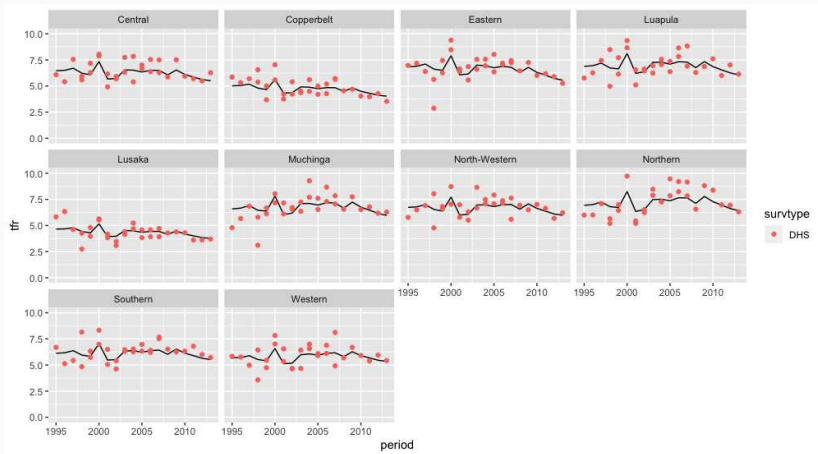


Figure 4: ZMB admin-1

